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and applies a (non-linear) activation function.

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Artificial neurons

an example



• A common activation function is logistic sigmoid function $f(x) = \frac{1}{1 + e^{-x}}$

• The output of the network becomes

Activation functions in ANNs

Σ f(·

hidden units

χm

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• The activation functions in MLP are typically continuous (differentiable) functions

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Result is a linear

transformation Then the unit applies a

non-linear activation function $f(\cdot)$

Output of the unit is

y = f(wx)

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For hidden units common choices are



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Activation functions in ANNs

- output units
 - The activation functions of the output units depends on the task. Common choices are
 - For regression, identity function
 - For binary classification, logistic sigmoid

$$P(y = 1 | x) = \frac{1}{1 + e^{-wx}} = \frac{e^{wx}}{1 + e^{-wx}}$$

- For multi-class classification, softmax

$$\mathsf{P}(\mathsf{y}=\mathsf{k}\,|\,\mathsf{x}) = \frac{e^{w_k \mathsf{x}}}{\sum_j e^{w_j \mathsf{x}}}$$

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MLP: a simple example



• Alternatively, we can write the computations in matrix form

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$$\begin{split} \mathbf{h} &= \mathbf{f}(W^{(1)}\mathbf{x}) \\ \mathbf{y} &= \mathbf{g}(W^{(2)}\mathbf{h}) \\ &= \mathbf{g}\left(W^{(2)}\mathbf{f}(W^{(1)}\mathbf{x})\right) \end{split}$$

 This corresponds to a series of transformations followed by elementwise (non-linear) function applications

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Solving non-linear problems with ANNs a solution to XOR problem

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Solving non-linear problems with ANNs $\ensuremath{\mathsf{a}}$ solution to XOR problem



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MLP: a simple example



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Solving non-linear problems with ANNs $\ensuremath{\mathsf{a}}\xspace$ solution to XOR problem



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Solving non-linear problems with ANNs a solution to XOR problem



Introduction Non-linearity MLP Non-linearity and MLP Learning in ANN's Solving non-linear problems with ANN's

a solution to XOR problem



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Non-linear activation functions are necessary

Without non-linear activation functions, an ANN with any number of layers is equivalent to a linear model.



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Error functions in ANN training

depend on the task

· For regression, a natural choice is the minimizing the sum of squared error

$$\mathsf{E}(w) = \sum_{i} (y_{i} - \hat{y}_{i})^{2}$$

• For binary classification, we use cross entropy

$$\mathsf{E}(w) = -\sum_{\mathfrak{i}} y_{\mathfrak{i}} \log \hat{y}_{\mathfrak{i}} + (1-y_{\mathfrak{i}}) \log(1-\hat{y}_{\mathfrak{i}})$$

· Similarly, for multi-class classification, also cross entropy

$$\mathsf{E}(w) = -\sum_{i}\sum_{k} y_{i,k} \log \hat{y}_{k}$$

In practice, the ANN loss functions will not be convex.

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Learning in multi-layer networks: the problem



We want a way to update non-final weights based on final error.

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Gradient descent: a refresher

• The general idea is to approach a minimum of the error function in small steps

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 $\boldsymbol{w} \leftarrow \boldsymbol{w} - \boldsymbol{\eta} \nabla J(\boldsymbol{w})$

 $-\nabla J$ is the gradient of the loss function, it points to the direction of the maximum increase $\boldsymbol{\eta}$ is the learning rate • The updates can be performed batch for the complete training set on-line after every training instance - this is known as *stochastic gradient descent* (SGD) mini-batch after small fixed-sized batches

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Global and local minima



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Learning in ANNs

- · ANNs implement complex functions: we need to use optimization methods (e.g., gradient descent) to train them
- Typically error functions for ANNs are not convex, gradient descent will find a local minimum
- · Optimization requires updating multiple layers of weights
- Assigning credit (or blame) to each weight during learning is not trivial
- An effective solution to the last problem is the backpropagation algorithm

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Calculating gradient on a neural network (with some simplification)



€€

дc

∂h1 ∂E

dc dh1



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Preventing overfitting in neural networks

• As in linear models, we can use L1 and L2 regularization by adding a regularization term to the error function (known as *weight decay*). For example,

 $J(w) = E(w) + \|W\|$

- · There are other ways to fight overfitting
 - With *early stopping*, one stops the training before it reaches to the smallest training error
 - With *dropout*, random units (with all of their connections) are dropped during training
 - Injecting noise at the output, as a way to (implicitly) model the noise in the target classes/values

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How many layers, units

- A network with single hidden layer is said to be *a universal approximator*: it can approximate any continuous function with arbitrary precision
- However, in practice multiple interconnected layers are useful and commonly used in modern ANN models
- The choice of layers, in general the architecture of the system, depends on the application

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Summary

- ANNs are powerful non-linear learners
 - based on some inspiration from biological NNs
 - using many simple processing units
 - built on linear models (logistic regression)
- For non-linear problems we need non-linear activation functions, and at least one hidden layer
- ANNs can be used for both regression and classification
- ANN loss functions are not convex, what we find is a local minimum
- They (typically) are trained with *backpropagation* algorithm Next:

Mon/Fri Unsupervised learning

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Stochastic gradient descent

- Standard (batch) gradient descent is computationally expensive: it updates weight at every *epoch*
- Stochastic gradient descent (SGD) updates weights for every training instance
- SGD may take more steps, but converges to the same solution
 - In practice a *mini-batch* is more common
 - Correct *batch size* is not only about efficiency, it also affects accuracy

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Adapting learning rate

• The choice of learning rate $\boldsymbol{\eta}$ is important

- too small slow convergence
 - too big overshooting may fluctuate around the minimum, or even jump away
 - The idea is to adapt the learning rate during learning
 - A common trick is adding a momentum: if we move in the same direction a long time accelerate

$$\Delta w_{ij}(t) = \eta \frac{\partial E}{\partial w_{ij}} + \alpha \Delta w_{ij}(t-1)$$

• There are many adaptive optimization algorithms: Adagrad, Adadelta, RMSprop, Adam, ...

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A bit of history

- 1950-60 ANNs (perceptron) became popular: lots of excitement in AI, cognitive science
- 1970s Not much interest
 - criticism on perceptron: linear separability
- 1980s ANNs became popular again
 - backpropagation algorithm
 - multi-layer networks
- 1990s ANNs had again fallen 'out of fashion'
 - Engineering: other algorithms (such as SVMs) performed generally better
 - From the cognitive science perspective: ANNs are difficult to interpret
- present ANNs (again) enjoy a renewed popularity with the name 'deep learning'

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Additional reading, references, credits

- Third edition (draft) of Jurafsky and Martin, has a new chapter on neural networks
- Hastie, Tibshirani, and Friedman (2009, ch.11) also includes an accessible introduction
- For a reivew of use of ANNs in NLP, including more advanced topics, see Goldberg 2016



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Additional reading, references, credits (cont.)

- Goldberg, Yoav (2016). "A primer on neural network models for natural language processing". In: Journal of Artificial Intelligence Research 57, pp. 345–420.
- Hastie, Trevor, Robert Tibshirani, and Jerome Friedman (2009). The Elements of Statistical Learning: Data Mining, Inference, and Prediction. Second. Springer series in statistics. Springer-Verlag New York. ISBN: 9780387648887. URL: http://web.stanford.edu/hastie/ElemStatLearn/.
- Jurefsky, Daniel and James H. Martin (2009). Speech and Language Processing: An Introduction to Natural Language Processing, Computational Linguistics, and Speech Recognition. second. Pearson Prentice Hall. isasc 978-0-13-504196-3.

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